

# An Improved Firefly Optimization Algorithm for Analysis of Arrhythmia Types

Mala Sinnor<sup>1</sup>, Shanthi Kaliyil Janardhan<sup>2</sup>

<sup>1</sup>Department of Electronics and Communication

Dr. Ambedkar Institute of Technology,

Bengaluru, India

malasinnor.ec@drait.edu.in

<sup>2</sup>Department of Medical Electronics

Dr. Ambedkar Institute of Technology,

Bengaluru, India

shanthikj.ml@drait.edu.in

**Abstract**— Irregular heartbeats rhythm is the result of arrhythmia condition which can be a threat to life if not treated at the early stage. If it is necessary to know the type of arrhythmia to treat the patient appropriately. The traditional method is complex and an efficient algorithm is required to diagnose. An improved firefly optimization algorithm is proposed to analyze arrhythmia types. Four performance measures confirm the model's effectiveness and experimental evaluation shows that it achieves a sensitivity of 86.27%, accuracy of 86.14%, precision of 87.52%, and specificity of 87.37% in arrhythmia-type classification. The algorithm can effectively classify the arrhythmia types with high accuracy and specificity.

**Keywords**- Improved Firefly Optimization Algorithm (IFOA), MLPT, EEMD, Lévy-flight firefly algorithm (LF-FA), Hjorth parameters

## I. INTRODUCTION

The electrical activity of heart is recorded by noninvasive device and the recorded signal is weak non-stationary ECG signal. While diagnosing different artifacts like baseline drift, electro-surgical noise, and electrode contact noise will get interfere and make it difficult to diagnose the arrhythmia type [3]. The importance of ECG signal in diagnosing arrhythmia is discussed in the research work.

A new Improved Firefly optimization Algorithm (IFOA) is presented to extract the features of the arrhythmia types. IFOA model uses MLPT and EEMD techniques for signal transformation and decompose the signal. Firefly optimization algorithm (FOA) extracts features using standard deviation, zero crossing rate, mean curve length, Hjorth parameters, mean teager energy, and log energy entropy [5-9] [11]. Feature reduction is also done by IFOA model by using intermittent scale-free search pattern i.e, Lévy flight style for optimal feature selection [12-14]. The research work shows the effectiveness and robustness of the IFOA model in terms of specificity, precision, sensitivity, and accuracy.

[15-16] The multi-class support vector machine (MSVM) is a machine learning method which depends on the Vapnik-Chervonenkis (VC) dimension theory and the other one is the structural risk minimization principle from statistical learning theory. Authors use different eigenvalues and Kernel functions of MSVM to classify normal heartbeat from atrial premature

contraction (APC), ventricular premature beat (VPC), right bundle branch block (RBBB), and left bundle branch block (LBBB). Training results will be different as the MSVM method depends on different kernel functions.

Saumendra et al. [19] used a random forest algorithm to detect tachycardia. The result shows the sensitivity and specificity of the classifier and further accuracy can be improved by modifying the technique. To overcome the drawback of entering the number of trees manually as a parameter, the researchers [18] introduced an enhanced random forest method that uses simulated annealing (SA) algorithm for an optimal number of trees calculation. The enhanced random forest method needs to be analysed with the other classifiers. A random forest network is proposed by Van Nam Pham [17], which is used to analyse and classify the ECG signals. The classified signals help to detect arrhythmias.

K-Nearest Neighbor (KNN) algorithm has been proposed by Indu Saini et al. [22] as a classifier to detect the QRS-complex in ECG signals. In addition to the detection, the authors try to find the accuracy, sensitivity, and specificity using KNN and found that the proposed algorithm is reliable and accurate for the detection of the QRS complex. Further, the algorithm can be enhanced to find the specific rhythms in ECG signals. [20] The authors performed ECG signal processing, feature extraction, and classifier as KNN to achieve the high accuracy of the proposed method when compared to other machine learning

algorithms. Toulmi Youssef et al. [21] used the discrete wavelet transform (DWT) as a mother wavelet with the Symlet 8 to establish the model with the classifier as the K Nearest Neighbors and found that the accuracy to identify the ECG signals is high.

Researchers proposed [23] Neural Networks methods such as CNN and RNN to classify the ECG signals accuracy of the proposed method is better when compared with the K-NN and SVM classifiers. To achieve high precision and accuracy machine learning methods need to be improved.

## II. METHODOLOGY

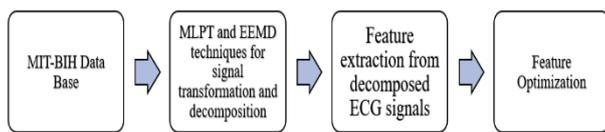


Fig. 1. Flow diagram of the proposed work

Arrhythmia refers to any irregularity in the rhythm or rate of the heartbeat, and [10] ECG signals are used to measure the electrical activity of the heart. The flow diagram of the proposed work is shown in Fig. 1, it includes four steps:

- The research work uses MIT-BIH arrhythmia databases, it consists recording of 48 different sets of heart diseases. Each recorded set is of 30 mins and sampled at a frequency rate of 360Hz [15].
- Signal Transformation and Decomposition: This step involves transforming the ECG signals into a format that is suitable for analysis and decomposing signals into component parts using two techniques: the Multilayer Perceptron Transform (MLPT) and the Ensemble Empirical Mode Decomposition (EEMD).
- Feature Extraction: This step involves extracting various features from the decomposed ECG signals, which are then used to classify arrhythmia types. The features include standard deviation, zero-crossing rate, Hjorth parameters, mean Teager energy, log energy entropy, and mean curve length.
- Feature Optimization: This step involves optimizing the extracted features using the Improved Firefly Optimization Algorithm (IFOA), which is a metaheuristic optimization algorithm.

The flow diagram shown in Fig 1., shows the framework of the proposed specifies the sequence of steps involved in the classification of arrhythmia types. The flow diagram visually represents the proposed framework, including the four steps mentioned above, as well as the inputs, outputs, and processing

of the data at each stage. The diagram is a useful tool to understand the proposed framework and the overall process involved in classifying arrhythmia types using ECG signals.

### A. MLPT-EEMD

The heart disease can be diagnosed by using noninvasive Electrocardiographic device which records electrical activity of heart. Arrhythmia can be detected at the early stage with help of these recordings. The recording contains important information which are complex and difficult to interpret. Multiscale Local Polynomial Techniques and Ensemble Empirical Mode Decomposition techniques are used for transformation and decomposition of the recorded ECG signals.

Multiscale Local Polynomial Techniques (MLPT) is wavelet transformation method used for non-equispaced data [4]. Complex signals are made simpler by multi-scale decomposition technique and it will smooth the signal during reconstruction. ECG signals are decomposed into number of Intrinsic mode functions (IMFs) by Empirical Mode Decomposition (EMD) technique [25-26]. In this method, high and low frequencies are decomposed into lower-order and higher-order IMFs components respectively. In general, low-frequency noises are by baseline wander and high-frequency noises are by power line interference, denoising of these signals is easily done by decomposing data. Further, the scale separation problem is overcome by Ensemble Empirical Mode Decomposition (EEMD) technique.

Complex ECG signals can be analysed using MLPT and EEMD and useful information is extracted for diagnosis of arrhythmia types. Fig 2. shows the result of decomposition and smoothing by MLPT and EEMD technique and process is as follows:

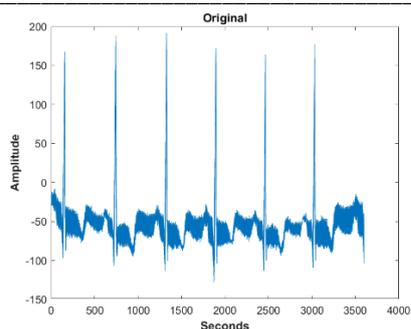
1. White noise  $n(t)$  is added in series to the input signal  $x(t)$ , then  $x_n(t) = x(t) + n(t)$
2. EMD algorithm decomposes the noisy signal  $x_n(t)$  into intrinsic mode functions (IMFs)
3. Steps 1 and 2 are repeated for N iterations to get  $IMF_k^i(t)$
4. Step 3 is repeated, in each trial series of white noise is considered to obtain the  $IMF_k^i(t)$ .

where  $IMF_k^i(t)$  is the  $k^{\text{th}}$  mode of the  $i^{\text{th}}$  trial;

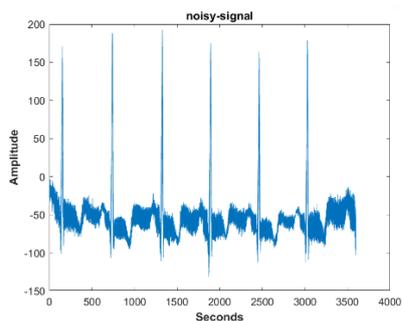
5. The ultimate Intrinsic Mode Functions (IMFs) are acquired by taking the average of the set of IMFs that correspond to each experiment as given by eqn. (1).

$$IMF_k(t) = \frac{1}{Nt} \sum_{i=1}^N IMF_k^i(t) \quad (1)$$

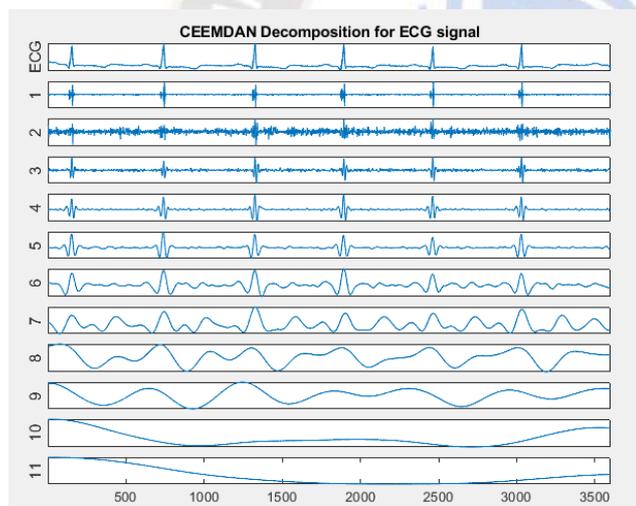
where N is the trials number.



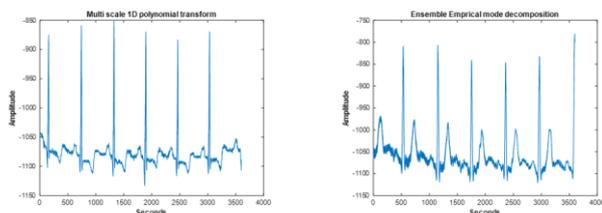
(a) Original ECG signal



(b) Noisy Signal



(c) Decomposed ECG signal



(d) MLTP-EEMD denoising signal

Fig 2. Result of MLPT-EEMD (a) Original ECG signal; (b) Noisy Signal; (c) Decomposed ECG signal; (d) MLTP-EEMD denoising signal

### B. Feature Extraction

After decomposing the ECG signals using MLPT and EEMD techniques, feature extraction is performed to capture different aspects of ECG signal. The following methods are used for feature extraction:

- The log energy entropy, which characterizes the non-linear dynamics of the ECG signal [30]. This technique allows to extract information about the heart's function and behavior of the ECG signal.
- Number of times the signal crosses the mean value within a three-second-long moving average [6] is counted using zero crossing rate technique. This technique provides information about the rate at which the ECG signal is changing over time.
- [7] Hjorth parameters technique, consists of three-time domain features: complexity, mobility, and activity. The activity is determined as the standard deviation of the epoch, and the mobility is defined as the ratio of the activity of the epoch to the derivative activity of the epoch. Complexity, on the other hand, is defined as the ratio of the activity of the epoch to the derivative mobility of the epoch. The Hjorth parameters provide information about the activity, mobility, and complexity of the ECG signal.
- The mean curve length [8], which is the linear distance between successive points on the curve. This technique provides information about the shape and smoothness of the ECG signal.
- Mean Teager energy [9], which is a non-linear operator and used to obtain energy of the signal based on mechanical and physical considerations. The Teager energy operator tracks the amplitude envelopes and instantaneous frequencies of the ECG signal, providing information about its energy content.
- Further, information about ECG signal is obtained by using continuous form of the Teager energy operator.

All these feature extraction techniques allow to capture a broad range of information about the ECG signal, including its non-linear dynamics, rate of change, activity, mobility, complexity, shape, and energy content.

The output of the Teager energy operator gives effective energy fluctuation because of its excellent time resolution. Finally, the standard deviation measures how far the ECG signals deviate from the mean value. The extracted 32 features are given to the improved IFOA for feature optimization that helps in decreasing the system complexity and computational time.

C. Feature Optimization

The Feature Optimization Algorithm (FOA) is a type of swarm intelligence algorithm which is encouraged by the flashing behavior of fireflies. The algorithm is designed to optimize the features extracted from ECG signals by mimicking the characteristics of firefly behavior. In the FOA, the population of fireflies represents the luminary flashing activity of fireflies, which is used to communicate, attract mates, and warn of predators.

The brightness value of the fireflies in the FOA is determined using the landscape of the objective functions. This value represents the fitness of the fireflies in the population. The fireflies are unisex, and each firefly is attracted to the other regardless of sex. The attractiveness of a firefly is proportional to its brightness value, meaning that less bright fireflies are attracted to more bright fireflies.

The FOA also considers the distance between fireflies in determining their attractiveness. As the distance between fireflies increases, their attractiveness and brightness decrease proportionally. This relationship is determined using absorptions and the inverse square law. The light intensity (I(x)) is mathematically defined in equation (4).

Overall, the FOA is a nature-inspired optimization algorithm that simulates the flashing behavior of fireflies to optimize the features extracted from ECG signals. By using the brightness value and attractiveness of fireflies, the FOA can effectively search for the optimal feature set for arrhythmia classification [11].

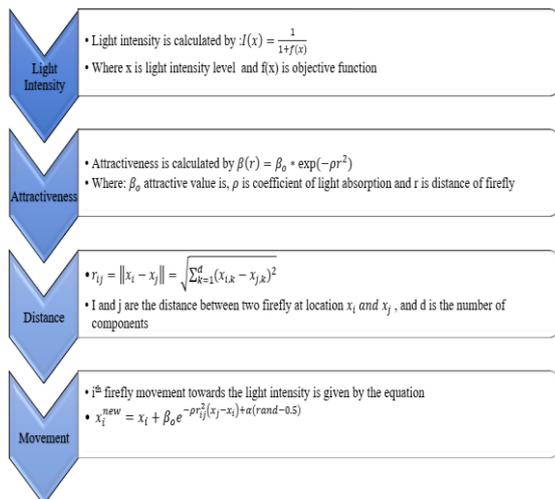


Fig 3. FOA algorithm

Firefly optimization algorithm usually gets trapped by the local optimization and this can be overcome by considering fruit flies navigate tricky landscapes by taking short, straight flights and then suddenly turning. This inspires another method called

the Lévy-flight firefly algorithm (LF-FA) that uses a similar pattern to explore more possibilities and find better solutions. Instead of always moving randomly in all directions, LF-FA uses a special type of randomness called Lévy distribution to decide which way to go. Therefore, the Improved Feature optimization algorithm (IFOA) has been developed using Lévy distribution and the updated position is by the given equation (2).

$$x_i^{new} = x_i + \beta_0 e^{-\rho r_{ij}^2} (x_j - x_i) + \alpha(\text{rand} - 0.5) \otimes \text{Lévy} \quad (2)$$

Where  $\alpha$  is the randomization parameter,  $\alpha(\text{rand} - 0.5)$  gives random direction,  $\otimes$  is the Hadamard product and the random step length is calculated by the Lévy flights. The Lévy flight distribution and the Lévy random number are specified in equations (3) and (4).

$$\text{Lévy}(\eta) \sim \mu = t^{1-\eta}, (0 \leq \eta \leq 2) \quad (3)$$

Random value for Lévy is calculated by,

$$\text{Lévy}(\eta) \sim \frac{\phi * \mu}{|\nu|^{1/\eta}} \quad (4)$$

Where  $\nu$  and  $\mu$  are the standard normal distributions, and  $\phi$  is calculated as follows in equation (5),

$$\phi = \left[ \frac{\tau(1 + \eta) * \sin\left(\frac{\pi\eta}{2}\right)}{\tau((1 + \eta)/2) * \eta x 2^{\eta + \frac{1}{2}}} \right]^{1/\eta} \quad (5)$$

Where  $\tau$  is standard Gamma function, and  $\eta = 1.5$

The research work is measured by four performances namely: specificity, precision, sensitivity, and accuracy. These measures are derived from four concepts: False Negative (FN), False Positive (FP), True Positive (TP), and True Negative (TN). Using these concepts, the accuracy, precision, sensitivity, and specificity are calculated as shown in equation (6), (7), (8) and (9) respectively to classify the arrhythmia type.

$$\text{Accuracy} = \frac{TN + TP}{TN + TP + FP + FN} \quad (6)$$

$$\text{Precision} = \frac{TP}{TP + FP} \quad (7)$$

$$\text{Sensitivity} = \frac{TP}{TP + FN} \quad (8)$$

$$\text{Specificity} = \frac{TN}{TN + FP} \quad (9)$$

III. QUANTITATIVE ANALYSIS

This section investigates the performance of the IFOA model on the MIT-BIH database. The analysis employs four classifiers, namely random forest, Multi-SVM (MSVM), CNN, Random Forest, and K-Nearest Neighbor (KNN). Simulation results for these classifiers, with and without the IFOA, are shown in Table

land 2. The IFOA model achieved better arrhythmia classification compared to other classifiers, with a sensitivity of 86.27%, accuracy of 86.14%, precision of 87.52%, and specificity of 87.37%. These simulation outcomes are higher than those obtained with traditional classifiers. Figure 4 and 5 shows performance of the classifiers with and without the IFOA.

TABLE 1. SIMULATION RESULTS OF THE CLASSIFIERS WITHOUT IMPROVED FIREFLY OPTIMIZATION ALGORITHM

Without IFOA				
Classifiers	MSVM	Random Forest	KNN	CNN
Accuracy (%)	85.58	93.08	89.86	88.72
Precision (%)	83.51	92.53	87.93	87.84
Sensitivity (%)	84.21	93.39	88.51	89.45
Specificity (%)	85.14	94.43	90.19	88.63

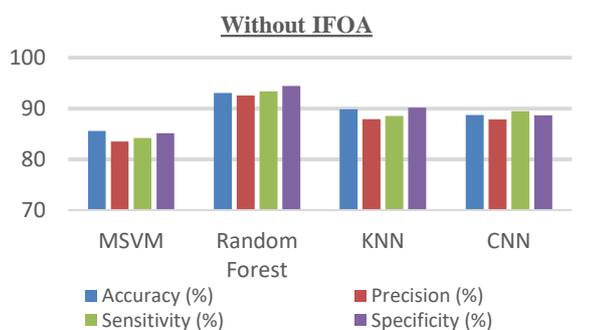


Fig. 4 Performance of classifiers without IFOA

TABLE 2. SIMULATION RESULTS OF THE CLASSIFIERS WITH IMPROVED FIREFLY OPTIMIZATION ALGORITHM

With IFOA				
Classifiers	MSVM	Random Forest	KNN	CNN
Accuracy (%)	86.14	95.03	90.99	81.50
Precision (%)	87.52	95.86	92.44	82.21
Sensitivity (%)	86.27	93.34	90.34	80.71
Specificity (%)	87.37	94.88	89.33	82.46

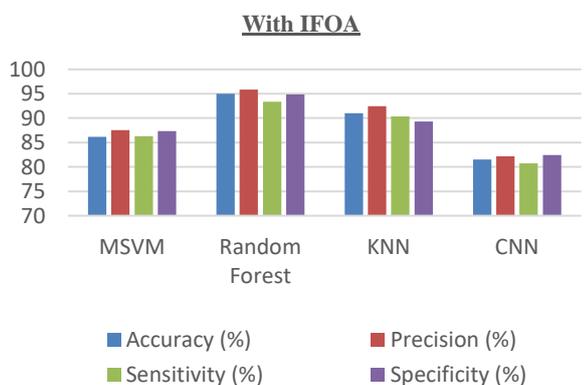


Fig. 5 Performance of classifiers with IFOA

## Conclusion

The manuscript implements the IFOA model to classify arrhythmia types effectively. The model comprises four major steps: signal transformation and decomposition, feature extraction, feature dimensionality reduction, and classification. MLPT and EEMD techniques are used to transform and decompose the ECG signals obtained from the MIT-BIH database. Feature extraction is performed using standard deviation, zero crossing rate, mean curve length, Hjorth parameters, mean teager energy, and log energy entropy. The IFOA method is then employed to optimize the multidimensional feature values, which enhances system complexity and computational time. Four performance measures confirm the model's effectiveness, and experimental evaluation shows that it achieves a sensitivity of 86.27%, accuracy of 86.14%, precision of 87.52%, and specificity of 87.37%. in arrhythmia type classification, outperforming existing models. Future work involves classifying the heart beats types by DNN model.

## ACKNOWLEDGMENT

The author wants to thank the research guide Dr. Shanthi K J for constant inspiration and valuable advice on improving the research work.

## REFERENCES

- [1] Thion Ming Chieng, Yuan wen Hau, Zaid Omar, "The study and comparison between various digital filters for ECG Denoising", IEEE-EMBS Conference on Biomedical Engineering and Sciences (IECBES) 2018.
- [2] Mala Sinnor, Shanthi K J, "Survey on Filtering Techniques Applied to ECG Signal", International Journal of Innovative Technology and Exploring Engineering (IJITEE) ISSN: 2278-3075, Volume-X, Issue-X, July 2019.
- [3] PanelSomaraju Boda, Manjunatha Mahadevappa, Pranab Kumar Dutta, "A hybrid method for removal of power line interference and baseline wander in ECG signals using EMD and EWT", Biomedical Signal Processing and Control, Volume 67, May 2021, 102466.
- [4] M. Sinnor and S.K. Janardhan, An ECG Denoising Method Based on Hybrid MLTP-EEMD Model, International Journal of Intelligent Engineering and Systems 15(1) (2022), 575-583. DOI: 10.22266/ijies2022.0228.52
- [5] Varsha Harpale, Vinayak Bairagi, "An adaptive method for feature selection and extraction for classification of epileptic EEG signal in significant states", Journal of King Saud University – Computer and Information Science, <https://doi.org/10.1016/j.jksuci.2018.04.014>
- [6] Majid Ali Khan Quaid, Ahmad Jalal, "Wearable sensors based human behavioral pattern recognition using statistical features and reweighted genetic algorithm", Multimedia Tools and Applications <https://doi.org/10.1007/s11042->

- 019-08463-7
- [7] Seung-Hyeon Oh, Yu-Ri Lee, Hyoung-Nam Kim, "A Novel EEG Feature Extraction Method Using Hjorth Parameter", *International Journal of Electronics and Electrical Engineering* 2(2):106-110, DOI:10.12720/ijeee.2.2.106-110
- [8] Reza Yahyaei, Tolga Esat Ozkurt, "Mean curve length: An efficient feature for brainwave biometrics", *Biomedical Signal Processing and Control* 76 (2022)
- [9] V. S. Mahalle, G. N. Bonde, S. S. Jadhao, and S. R. Paraskar, "Teager Energy Operator: A Signal Processing Approach for Detection and Classification of Power Quality Events", *Proceedings of the 2nd International Conference on Trends in Electronics and Informatics (ICOEI 2018)* IEEE Conference Record: # 42666; IEEE Xplore ISBN:978-1-5386-3570-4
- [10] Varun Gupta, Monika Mittal, Vikas Mittal, Arvind Kumar Sharma, Nitin Kumar Saxena, "A novel feature extraction-based ECG signal analysis", *J. Inst. Eng. India Ser. B* (October 2021) 102(5):903-913 <https://doi.org/10.1007/s40031-021-00591-9>
- [11] C. Kamath, "ECG beat classification using features extracted from Teager energy functions in time and frequency domains", *IET Signal Process.*, 2011, Vol. 5, Iss. 6, pp. 575-581 575 doi: 10.1049/iet-spr.2010.0138
- [12] Alan S. Said Ahmad, Salah Matti , Adel Sabry Essa, Omar A.M. ALhabib, Sabri Shaikhow , "Features Optimization for ECG Signals Classification", (*IJACSA*) *International Journal of Advanced Computer Science and Applications*, Vol. 9, No. 11, 2018 383.
- [13] Dr. S.A. Sivakumar. (2019). Hybrid Design and RF Planning for 4G networks using Cell Prioritization Scheme. *International Journal of New Practices in Management and Engineering*, 8(02), 08 - 15. <https://doi.org/10.17762/ijnpme.v8i02.76>
- [14] Dr. Padmavathi Kora, "ECG based Myocardial Infarction Detection using Hybrid Firefly Algorithm", *Computer Methods and Programs in Biomedicine*, March 2017, DOI: 10.1016/j.cmpb.2017.09.015
- [15] Sofiah Ishlakhul Abda, Auli Damayanti & Edi Winarko, "Detection of Heart Abnormalities Based On ECG Signal Characteristics using Multilayer Perceptron with Firefly Algorithm-Simulated Annealing", *Contemporary Mathematics and Applications* Vol. 3, No. 1, 2021, pp. 45-55.
- [16] Tonghui Li, Jieming Ma, Xinyu Pan, Yujia Zhai, and Ka Lok Man, "Classification of Arrhythmia using Multi-Class Support Vector Machine", *Proceedings of the International MultiConference of Engineers and Computer Scientists 2017 Vol II, IMECS 2017*, March 15 - 17, 2017, Hong Kong
- [17] Tharun J. Iyer, B. Kishan & Ruban Nersisson, "Prediction and Classification of Cardiac Arrhythmia Using a Machine Learning Approach", *International Conference on Automation, Signal Processing, Instrumentation and Control*, *Advances in Automation, Signal Processing, Instrumentation, and Control* pp 603-610 i-CASIC 2020
- [18] Van Nam Pham, Hoai Linh Tran, "Electrocardiogram (ECG) Circuit Design and Using the Random Forest to ECG Arrhythmia Classification", *International Conference on Engineering Research and Applications ICERA 2022: Advances in Engineering Research and Application* pp 477-494
- [19] Sihem NITA; Salim BITAM; Abdelhamid MELLOUK, "An Enhanced Random Forest for Cardiac Diseases Identification based on ECG signal", *International Wireless Communications & Mobile Computing Conference (IWCMC)*, June 2018, ISSN: 2376-6506, IEEE, DOI: 10.1109/IWCMC.2018.8450361
- [20] Saumendra Kumar Mohapatra, Tripti Swarnkar, Mihir Narayan Mohanty, "Design of Random Forest Algorithm Based Model for Tachycardia Detection", *Advanced Computing and Intelligent Engineering*, pp 191-199
- [21] B. Venkataramanaiah, J. Kamala, "ECG signal processing and KNN classifier-based abnormality detection by VH-doctor for remote cardiac healthcare monitoring", *Soft Computing* (2020) 24:17457-17466 <https://doi.org/10.1007/s00500-020-05191-1>
- [22] Toulmi Youssef, Belhoussine Drissi Taoufiq, Benayad Nsiri, "ECG signal diagnosis using Discrete Wavelet Transform and K-Nearest Neighbor classifier", *The 4th International Conference on Networking, Information Systems & Security*, Kenitra, April 202, DOI:10.1145/3454127.3457628
- [23] Mwangi, J., Cohen, D., Costa, R., Min-ji, K., & Suzuki, H. Optimizing Neural Network Architecture for Time Series Forecasting. *Kuwait Journal of Machine Learning*, 1(3). Retrieved from <http://kuwaitjournals.com/index.php/kjml/article/view/132>
- [24] Indu Saini, Dilbag Singh, Arun Khosla, "QRS detection using K-Nearest Neighbor algorithm (KNN) and evaluation on standard ECG databases", *Journal of Advanced Research*, (2013) 4, 331-344, doi.org/10.1016/j.jare.2012.05.007
- [25] Muhammad Rausan Fikri, Indah Soesanti, Hanung Adi Nugroho, "ECG Signal Classification Review", *IJITEE (International Journal of Information Technology and Electrical Engineering)*, Vol. 5, No. 1, June 2021, DOI:10.22146/ijitee.60295
- [26] Krishna Teja, Rahul Tiwari and Satish Mohanty "Adaptive denoising of ECG using EMD, EEMD and CEEMDAN signal processing techniques", *Journal of Physics: Conference Series* 1706 (2020) 012077, IOP Publishing, doi:10.1088/1742-6596/1706/1/012077
- [27] Dengyong Zhang , Shanshan Wang, Feng Li, Shang Tian, Jin Wang, Xiangling Ding, and Rongrong Gong , "An Efficient ECG Denoising Method Based on Empirical Mode Decomposition, Sample Entropy, and Improved Threshold Function", *Hindawi Wireless Communications and Mobile Computing* Volume 2020, Article ID 8811962, 11 pages <https://doi.org/10.1155/2020/8811962>

- [28] Lahcen El Bouny · Mohammed Khalil · Abdellah Adib, “Ecg Signal Filtering Based On Ceemdan With Hybrid Interval Thresholding And Higher Order Statistics To Select Relevant Modes”, May 2019 Multimedia Tools And Applications 78(6). Doi:10.1007/S11042-018-6143-X
- [29] Mehrnoosh Sadat Safi , Seyed Mohammad Mehdi Safi, “Early detection of Alzheimer’s disease from EEG signals using Hjorth parameters”, Biomedical Signal Processing and Control, 2021, <https://doi.org/10.1016/j.bspc.2020.102338>
- [30] Gunjal, M. B. ., & Sonawane, V. R. . (2023). Multi Authority Access Control Mechanism for Role Based Access Control for Data Security in the Cloud Environment. International Journal of Intelligent Systems and Applications in Engineering, 11(2s), 250 –. Retrieved from <https://ijisae.org/index.php/IJISAE/article/view/2623>
- [31] Xin-She Yang, “Firefly Algorithm, Lévy Flights and Global Optimization”, Research and Development in Intelligent Systems XXVI pp 209–218, Springer
- [32] J. Wu, Y.-G. Wang, K. Burrage, Y.-C. Tian, B. Lawson and Z. Ding, An improved firefly algorithm for global continuous optimization problems, Expert Systems with Applications 149 (2020), 113340. <https://doi.org/10.1016/j.eswa.2020.113340>

