

Power penalty and CNR penalty Performance in Single-Tone Radio-over-Fiber Transmission system using OSSB Technique due to Phase Noise from Laser-Spectral Width

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Abstract—In this paper, we analysed the effect of noise due to linewidths of laser on single-tone radio-over-fiber (RoF) transmission system. A Mach-Zehnder modulator (MZM) and a phase shifter are employed to externally generate an optical single sideband (OSSB) signal since the OSSB signal is tolerable for power degradation due to a chromatic fiber-dispersion effect. It is shown that Power penalty and CNR penalty is increased exponentially when we change laser linewidth (γ_{RF}) from 10 MHz to 624 MHz. The results are calculated for transmission distance (L_{FIBER}) 10 km to 40 km for optical single sideband (OSSB)-RoF transmission system. We investigate the effect of laser linewidth with 30-GHz RF carrier (f_{RF}), fiber dispersion parameter (D) 17 ps/nm-km, and 1550-nm laser (λ) with zero linewidth.

Key words—carrier-to-noise ratio (CNR), direct detection, fiber, Bandwidth, laser, line width, Dual electrode Mach-Zehnder modulator (DEMZM), optical single sideband (OSSB), oscillator, phase noise, power spectral density (PSD), radio.

1. Introduction

Wireless broadband, fixed and mobile, can be found almost everywhere, and it became a part of our modern life style. The data traffic in telecommunication networks has been growing tremendously over recent years, and experts predict accelerating data volumes from today three Exabyte a year to ninety Exabyte per year by 2015, where an Exabyte is equal to one million terabytes [23]. For fulfilling the demands, wideband communication systems are necessary in both wired link and wireless link. Radio-over fiber (RoF) systems have been good candidates for broadband services. This is a technology, which modulates light into radio frequency and transmits it via optical fiber to facilitate wireless access. Radio signals are carried over fiber utilising distributed antenna systems in fiber-optic cellular and micro-cellular radio networks. Radio signals in each cell are transmitted and received to and from mobile users by applying a separate little box that is connected to the base station via optical fiber. Cells are divided into microcells to enhance the frequency re-use and support a growing number of mobile users.

The introduction of microcells has the following advantages. Firstly, the microcell is able to meet increasing bandwidth demands; secondly, reduces the power consumption also the size of the handset devices. The high-power radiating base station antenna is replaced by a divided antenna system connected to the base station via optical fiber [24]. However, the performance of RoF systems depends on the method used to generate the optically modulated radio frequency (RF) signal, power degradation due to fiber chromatic dispersion, nonlinearity due to an optical power level, and phase noise from a laser and an RF oscillator [1-14]. There are two techniques to generate the optically

modulated RF signal: Direct and External modulation. The direct modulation scheme is simple but suffers from a laser-frequency chirp effect, and this chirp effect results in severe degradation of the system performance. However, this can be eliminated by using the external-modulation scheme instead of the direct modulation scheme [2]. Although the external-modulation scheme is employed, the conventional optical double sideband (ODSB) signal can degrade the received RF signal power due to fiber chromatic dispersion drastically. For overcoming the power degradation, an optical single sideband (OSSB) signal, generated by using a phase shifter and a dual-electrode (DE) Mach-Zehnder modulator (MZM), is employed [2].

In addition to these two effects, the nonlinearity of an optical fiber can give a large penalty on the long-haul transmission and multichannel system using a high-power signal. For the high-power transmission, the nonlinear effect should be managed by utilizing a modulation format [3], and by controlling the launched power level [4]. The nonlinear effect, however, can be negligible in short and low optical power less than 0 dBm, especially for a single channel transmission. Unlike those parameters, phase noise is one of the practical and decisive factors in high-quality services that require high signal-to-noise ratio (SNR), because it results in a bit error rate (BER) floor in a high SNR value [6]. This phenomenon is serious to RoF systems because the purpose of RoF systems is to provide a service of high data rate and high quality, which require a large SNR. Thus, the system performance can be more sensitive to the phase noise in these services. The influence of the phase noise on optical communication systems has been investigated [5]–[10]. Kitayama et al. analyzed the system performance for an ODSB signal including laser phase noise and suggested how to compensate the differential delay by using a dispersion-

compensating fiber (DCF). He focused on how to compensate fiber chromatic dispersion for the ODSB signal experimentally and analytically. Barry and Lee [6] and Salz [7] analyzed the performance of coherent optical systems with laser phase noise by utilizing a Wiener process, since coherent detection provides better sensitivity than that of direct detection, while direct detection has a simple structure [21]. Gallion and DeBarge [8] and Tkach [9] used an autocorrelation function and a PSD function for evaluating the effect of the laser line width and fiber chromatic dispersion on the system performance. Gallion analyzed the power spectral density (PSD) function of a photocurrent incorporating the laser phase noise in detail. Gliese applied the result in [8] to study the influence of chromatic fiber dispersion on the transmission distance of fiber optic microwave and millimeter wave links [10]. For the tolerance to fiber chromatic dispersion, dual correlated lasers were employed to generate an OSSB signal in [10]. In this paper, we will analyse the CNR penalty and Power penalty due to fiber chromatic dispersion and phase noises from a laser using an OSSB signal and a direct-detection scheme. For the analysis of the Power penalty and CNR penalty, the autocorrelation and the PSD function of a received photocurrent are evaluated. The bandwidth of an electrical filter is dealt in the Penalty since the phase noises result in an increase of the required bandwidth and the increased bandwidth causes an additional CNR and Power penalty. It is shown that the phase noise from the Laser Diode is more dominant in long haul transmission because differential delay is more (>100ps) at 40km as compared to 2km, as the distance increases Power penalty and CNR increases exponentially, Since at short distances the phase noise due to laser is not much as compared to RF oscillator.

2. R-o-F Architecture

In a RoF system an optically modulated radio frequency signal is generated from a central office (CO) to a base station (BS) via an optical fiber. An OSSB signal is produced by using a Dual-Electrode Mach-Zehnder modulator (DEMZM) and a 90° phase shifter, and optically modulated by LASER diode and DEMZM. The optically modulated signal is transmitted to BS where it receives RF signal is recovered by using a photodetector (PD) and a BPF arrives at a user terminal (UT) through a wireless channel as shown in fig.1.

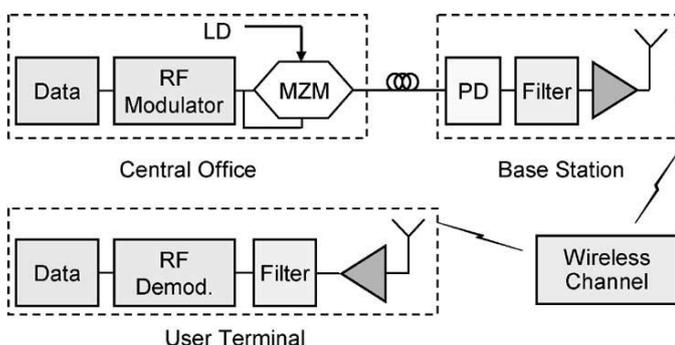


Fig.1

The optical signals from the laser and the RF oscillator are represented mathematically as

$$x_{LD}(t) = A \cdot \exp(j(\omega_b(t) + \Phi_{LD}(t))) \tag{1}$$

$$x_{RF}(t) = V_{RF} \cdot \cos(\omega_f(t) + \Phi_{RF}(t)) \tag{2}$$

Where A and V_{RF} are amplitudes of signals from the LD and the RF oscillator

respectively, ω_b and ω_f are angular frequencies of the signals from the LD and the RF oscillator, Φ_{LD} and Φ_{RF} are phase-noise processes and Φ_{LD} is characterized by a Wiener process [6] as

$$\Phi_{LD}(t) = \int_0^t \Phi_{\dot{b}}(\tau) d\tau \tag{3}$$

The time derivative $\Phi_{\dot{b}}(t)$ is not flat at low frequencies due to 1/f noise [6]. The white phase noise, however, is the principal cause for line broadening and is associated with quantum fluctuations [7]. Thus, $\Phi_{LD}(t)$ can be modeled as a zero-mean white Gaussian process with a PSD [6]

$$S_{\Phi_{\dot{b}}}(\omega) = 2\pi\Delta\nu_{LD} \tag{4}$$

Where ν_{LD} is Laser linewidth

After optically modulating $x_{LD}(t)$ by $x_{RF}(t)$ with a DEMZM and by controlling the phase shifter, the OSSB signal is generated by setting θ (phase shift) and γ (normalized dc value of LD) to 90° and 0.5, respectively, and this OSSB signal at the output of DEMZM is represented as

$$E(0, t) = A \cdot L_{MZM} \left[J_0(\alpha\pi) \cdot \exp(j(\omega_b(t) + \Phi_{LD}(t) + \frac{\pi}{4})) - \sqrt{2} J_1(\alpha\pi) \cdot \exp(j(\omega_b(t) + \Phi_{LD}(t) + \omega_f(t) + \Phi_{RF}(t))) \right] \tag{5}$$

Where $\alpha = V_{RF}/\sqrt{2}V_{\pi}$ is the normalized dc value, V_{π} is the switching voltage of the DEMZM, L_{MZM} is the insertion loss of the DEMZM, and θ is the phase shift by the phase shifter. Generally, $V_{\pi} \gg V_{RF}$, thus, the high-order components of the Bessel function are neglected.

2. Power Penalty and Carrier to Noise Ratio Penalty Analysis

After transmitting the OSSB at the output of DEMZM through standard single-mode fiber (SSMF) of L_{FIBER} Km is represented as

$$E(L, t) = A \cdot L_{MZM} \cdot L_{LOSS} \cdot 10^{-\frac{\alpha_{FIBER} \cdot L_{FIBER}}{20}} \cdot J_0(\alpha\pi) \left[\exp(j(\omega_b(t) + \Phi_{LD}t - \tau_0 - \Phi_1 + \pi/4 - 2J_1\alpha\pi/0\alpha\pi \cdot \exp(j\omega_{LD}t + \Phi_{LD}t - \tau + \omega_{RF}t + \Phi_{RF}t - \tau + \Phi_2)) \right] \tag{6}$$

Where L_{LOSS} denotes an additional loss in the optical link line, α_{FIBER} is the SSMF loss, L_{FIBER} is the transmission distance of the SSMF, and τ_0 and τ_+ define group delays for a center angular frequency of $\omega_b(t)$, and an upper sideband frequency of $\omega_b(t) + \omega_f(t)$, Φ_1 and Φ_2 are phase-shift parameters for specific frequencies due to the fiber chromatic dispersion. By using a square-law model, the photocurrent $i(t)$ can be obtained from (6) as follows

$$i(t) = R|E(L, t)|^2 = RA_1^2 [B + 2\alpha_1 \cos(\omega_f(t) + \Phi_{LD}(t - \tau_+) - \Phi_{LD}(t - \tau_0) + \Phi_{RF}(t - \tau_+) - \Phi_2 + \Phi_1)] \tag{7}$$

Where $A_1 = A \cdot L_{MZM} \cdot L_{LOSS} \cdot 10^{-\frac{\alpha_{FIBER} \cdot L_{FIBER}}{20}} \cdot J_0(\alpha\pi)$

$$\alpha_1 = \frac{\sqrt{2}J_1(\alpha\pi)}{J_0(\alpha\pi)}, B = 1 + \alpha_1^2, R = \text{Responsivity of PD}$$

From (7), the autocorrelation function $R_{AF}(\tau)$ is obtained as

$$R_{AF}(\tau) = \langle i(t) \cdot i(t + \tau) \rangle \tag{8}$$

$$\frac{R_{AF}(\tau)}{R^2 A_1^4} = B^2 \cdot \begin{cases} 2 \cdot \alpha_1^2 \cdot \cos(\frac{\pi}{2} \tau) \exp(-2\gamma_1 |\tau|), & |\tau| \leq \tau_1 \\ 2 \cdot \alpha_1^2 \cdot \cos(\frac{\pi}{2} \tau) \exp(-2\gamma_{LD} \tau_1 - \gamma_{RF} |\tau|), & |\tau| > \tau_1 \end{cases} \tag{9}$$

Where $\Delta\nu_{LD}$ and $\Delta\nu_{RF}$ are the line widths for the laser and the RF oscillator, respectively, $2\gamma_{LD} (= 2\pi\Delta\nu_{LD})$ and $2\gamma_{RF} (= 2\pi\Delta\nu_{RF})$ are the angular full-line width at half-maximum (FWHM) of the Lorentzian shape for the laser and the RF oscillator, respectively, and $2\gamma_t$ is related to the total line width. Note that the $2\gamma_t$ is given not as $2\pi\Delta\nu_{LD} + 2\pi\Delta\nu_{RF}$ but $2\pi\Delta\nu_{LD} + \pi\Delta\nu_{RF}$. Now $\tau_1 (= \tau_+ - \tau_0)$ is the differential delay due to the fiber chromatic dispersion and is dependent on the wavelength λ , the carrier frequency f_{RF} , the fiber chromatic dispersion D , and the optical transmission distance L_{FIBER} . It is given by [10]

$$\tau_1 = D \cdot L_{FIBER} \cdot \lambda^2 \cdot \frac{f_{RF}}{c} \tag{10}$$

where c is the light velocity.

The shot noise term at the PD is omitted here since the noise power can be evaluated by the product of bandwidth and noise density level. The PSD function of the photocurrent is given by the Fourier transform of Autocorrelation Function.

$$S(f) = F \langle R_{AF}(\tau) \rangle$$

$$\frac{S(f)}{R^2 A_1^4} = B_2 \cdot \delta(f) + G(f - f_{RF}) + G(f + f_{RF})$$

Where

$$G(f - f_{RF}) = S_1 + S_2 + S_3$$

After getting the three terms, S_1 and S_2 defines the broadening effects due to the fiber chromatic dispersion and the line width of the laser and the RF oscillator. By using Fourier Transform the received RF carrier power $P_{RECEIVED}$ is approximately represented as follows

$$P_{RECEIVED} = \frac{4R^2 A_1^4 \alpha_1^2}{\pi} e^{-2\gamma_t \tau_1} \cdot \tan^{-1} \left(\frac{\pi \cdot B_{RF}}{\gamma_{RF}} \right) \tag{11}$$

Where $2\gamma_t \tau_1 \ll 1$ and $\gamma_t \ll \gamma_{RF}$. This is because the laser linewidth is much greater than the RF oscillator linewidth. The received RF carrier power is a function of the differential delay τ_1 , the laser and the RF oscillator linewidths, and the Bandwidth of the electrical filter B_{RF} . The ratio between the bandwidth and the linewidth of the RF oscillator is one of the dominant parameters for the

carrier power. Practical systems employ various types of bandwidth as the required power, such as half-power bandwidth, fractional-power containment bandwidth (99% of signal power), and so on [17]. For evaluating the total RF power excluding dc power, we utilize the Autocorrelation Function.

$$P_{TOTAL} = R_{AF}(0) - R^2 A_1^4 B^2$$

$$P_{TOTAL} = 2R^2 A_1^4 \alpha_1^2 \tag{12}$$

By using (12), we define the ratio p between the total carrier Power and the required power as follows

$$p = \frac{P_{RECEIVED}}{P_{TOTAL}} \text{ for } 2\gamma_t \tau_1 \ll 1 \text{ and } \gamma_t \ll \gamma_{RF}$$

$$p \cong \frac{2}{\pi} e^{-2\gamma_t \tau_1} \cdot \tan^{-1} \left(\frac{\pi \cdot B_{RF}}{\gamma_{RF}} \right) \tag{13}$$

Required bandwidth for ratio p is

$$B_{RF} = \frac{\gamma_{RF}}{\pi} \cdot \tan \left(\frac{\pi}{2} e^{2\gamma_t \tau_1} p \right) \tag{14}$$

When we need more received signal power the required bandwidth increases. We use $2B_{RF}$ instead of B_{RF} because received power is in real and also in imaginary part. Similarly noise is evaluated. Now and Carrier to noise ratio can be calculated by using (11) and (14).

$$\frac{C}{N} = \frac{\text{Carrier Power}}{\text{Noise Power}}$$

$$\frac{C}{N} = \frac{P_{RECEIVED}}{2B_{RF} \frac{N_0}{2}}$$

$$\frac{C}{N} = \frac{2R^2 A_1^4 \alpha_1^2 p}{N_0 \frac{\gamma_{RF}}{\pi} \tan \left(\frac{\pi}{2} e^{2\gamma_t \tau_1} p \right)} \tag{15}$$

Now from (13) and (15) the Power penalty, CNR penalty induced by the Differential delay from the fiber chromatic dispersion by varying laser linewidth is as

$$\text{Power Penalty} = \frac{1}{p} = 1 / \left(\frac{2}{\pi} e^{-2\gamma_t \tau_1} \cdot \tan^{-1} \left(\frac{\pi \cdot B_{RF}}{\gamma_{RF}} \right) \right) \tag{16}$$

$$\begin{aligned} \text{carrier to noise ratio penalty} &= \Delta \frac{C}{N} \\ &= 10 \log_{10} \left(\frac{(C/N)_0}{(C/N)} \right) \\ &= 10 \log_{10} \left(\frac{p_0 \cdot \gamma_{RF} \tan \left(\frac{\pi}{2} e^{2\gamma_t \tau_1} p \right)}{p \cdot \gamma_{RF_0} \tan \left(\frac{\pi}{2} e^{\gamma_{RF_0} \tau_1} p_0 \right)} \right) \end{aligned}$$

(17)

To calculate the CNR_0 , set $p_0=0.5$, $\gamma_{RF_0} = \pi$, it means 1-Hz linewidth of the RF oscillator, and zero laser linewidth. we set $D=17$ ps/nm · km, $\lambda=1550$ -nm.

3. Results

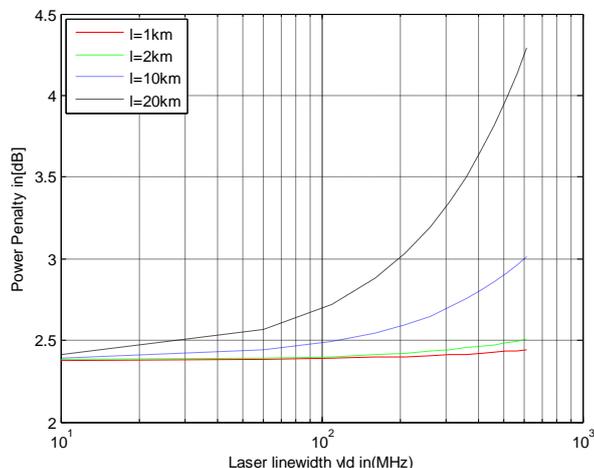


Fig.2

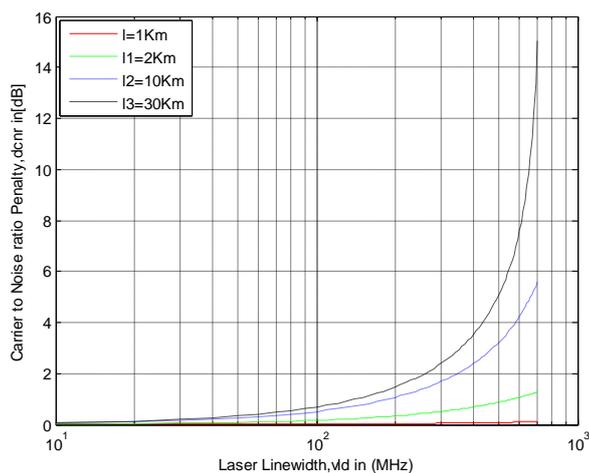


Fig.3

The result of the laser-line width effect is described in Fig.2&3 using (16) and (17). The penalties are observed for laser line width from 10 to 624 MHz since 10 and 624 MHz are typical line width values of a distributed-feedback (DFB) laser and a Fabry-Pérot (FP) laser [18]. Δ CNR and power penalty exponentially increases as the laser linewidth. Therefore, the RoF system relatively suffers from both penalty for a long transmission, such as 30 km, while both are almost unchanged for the FP laser in the short-transmission case (=2 km). We can say that the FP laser can be used in a practical microcell boundary because the radius of the microcell is from 0.2 to 1 km [20].

4. Conclusion & Discussion

We have seen that the Power Penalty and carrier-to-noise ratio (CNR) penalty due to the limits of the fiber chromatic dispersion in the standard single-mode fiber (SSMF) and the phase noises of the laser in the radio-over-fiber (RoF) system.

In order to investigate the penalties, we evaluate the power spectral density (PSD) function, and the PSD function is identical with the previous result in [8], when the phase noise of the RF oscillator is 0. A practical laser having nonzero linewidth induces penalties by the multiplication with nonzero differential delay in the RoF system that uses external modulation with a (DEMZM) dual-electrode Mach-Zehnder modulator and direct detection. However, the penalty due to the laser linewidth is much less than the penalty due to the RF-oscillator linewidth at short distance. The penalties come from the power degradation due to phase noises and the differential delay caused by fiber chromatic dispersion. The filter bandwidth at an electrical receiver should be selected carefully considering tradeoff between the penalties and required signal power ratio p , especially for p greater than 0.9, since the increase of bandwidth causes the increase of noise power. The penalties for the use of a 99% bandwidth filter are 15.1 dB, as compared to the case using the half-power bandwidth. The CNR penalty due to the FP laser linewidth is only 0.22 dB in a microcell (2 km) even though it becomes relatively severe in a long distance (30 km). The long-haul transmission is different because the initial phase difference is not maintained at the end of the optical fiber anymore. The observed linewidth due to the laser at the PD will be twice that of an initial laser linewidth Φ_{LD} since the differential delay is much greater than the coherence time. Therefore, the phase noise processes of Φ_{LD} and $\Phi_{LD}(t + \tau_1)$ are completely uncorrelated [9]. In that case, the system performance will suffer from the laser linewidth in a long-haul case seriously while the laser-line-width effect can be ignored in a short transmission. In conclusion, the bandwidth of an electrical filter at the receiver should be carefully chosen considering minimum required signal power ratio p and CNR penalty at the same time.

7. References

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